

$B_{(s)} \rightarrow V\gamma$ and $B_{(s)} \rightarrow A\gamma$ decays in PQCD approach

李润辉

Based on: W . Wang ¹, R.H. Li ^{2;1} and C.D. Lu ¹, arXiv: 0711.0432.

¹ Institute of High Energy Physics

² Physics Department of Shandong University

Menu

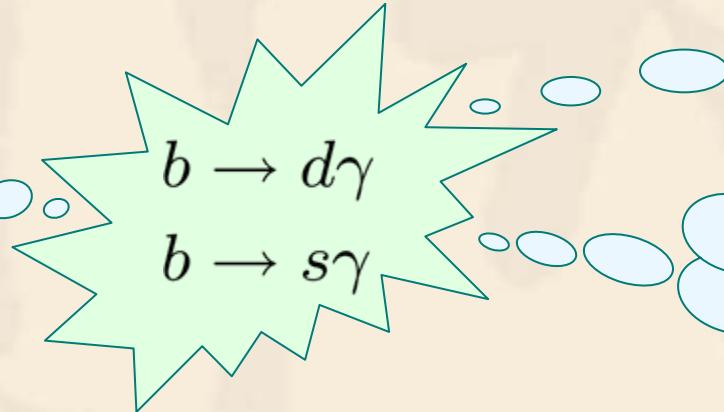
- ❖ Brief introduction
- ❖ Calculation
 - Form factors
 - Br & CPV & etc
- ❖ Summary

Introduction

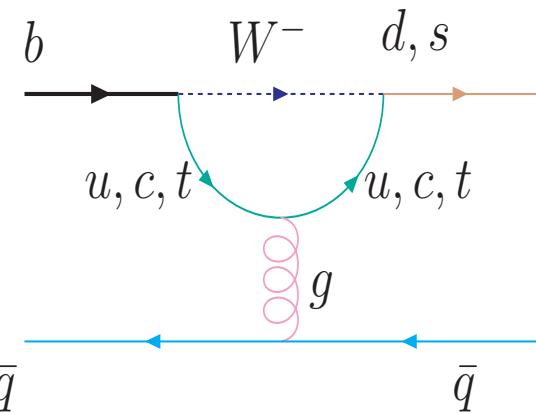
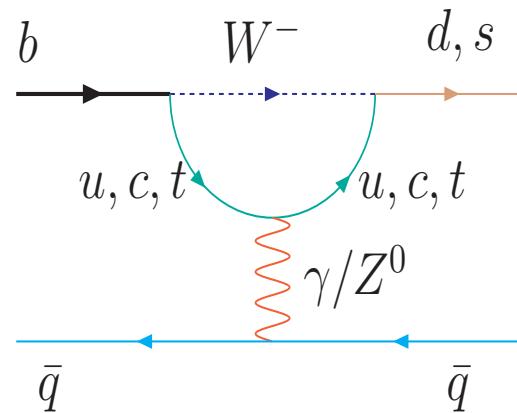
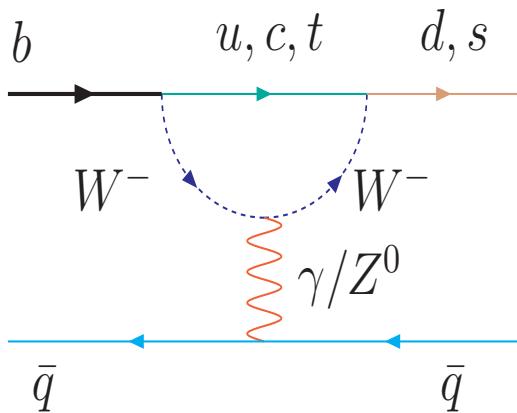
Dominated
by FCNC

Loop
effects in
SM

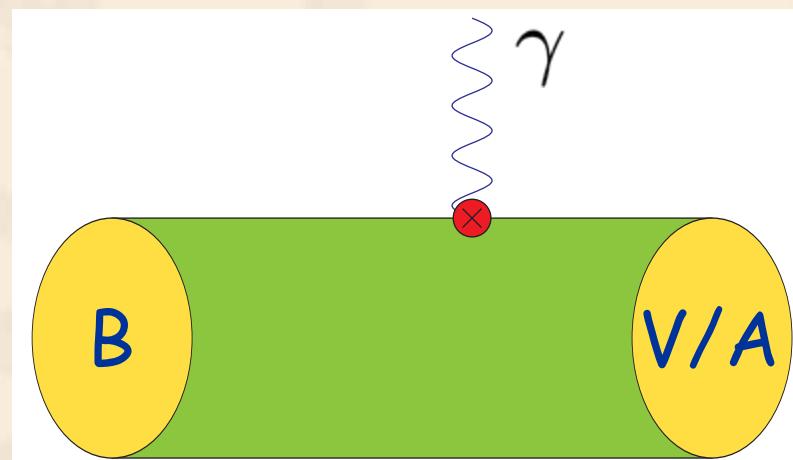
Ideal probe
for new
physics



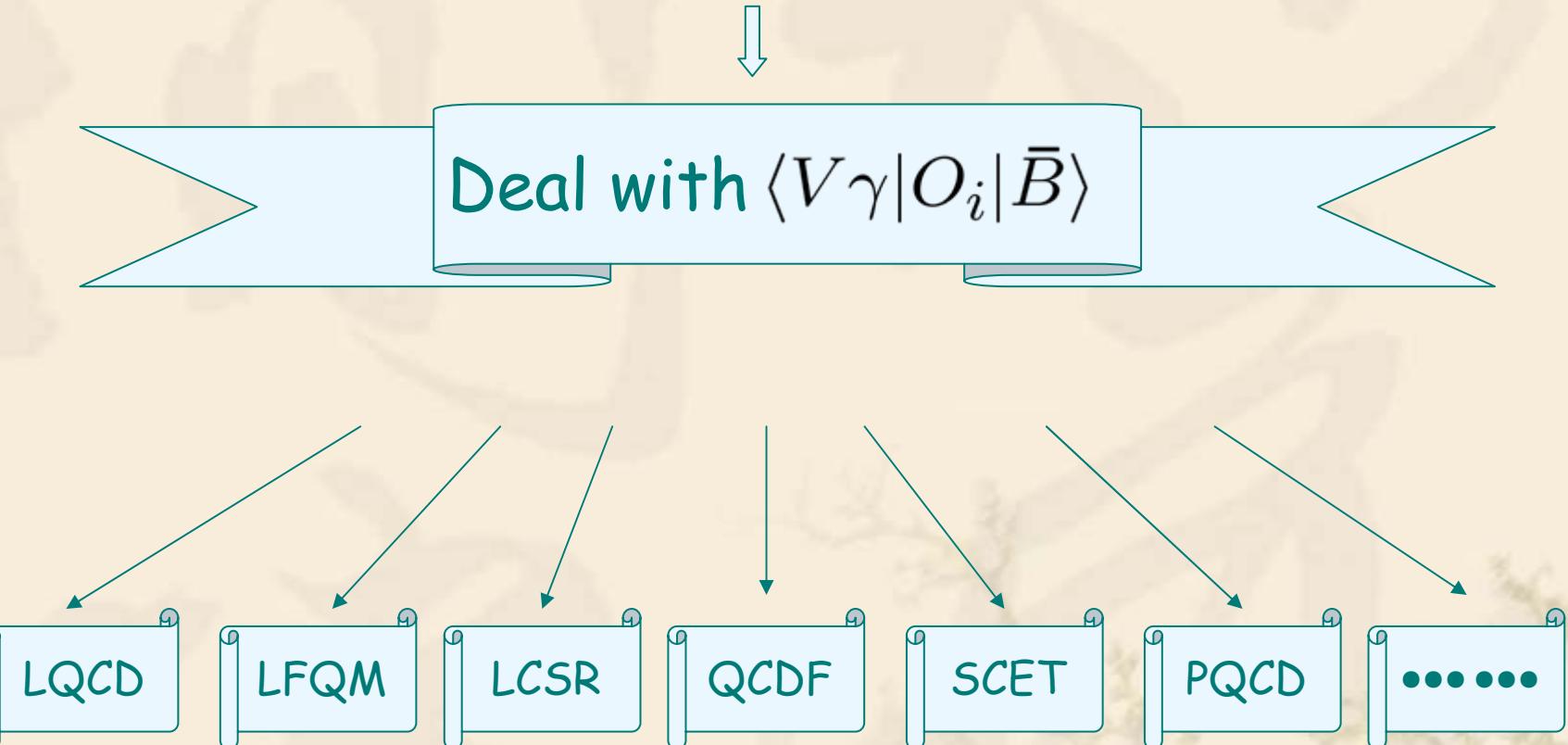
FCNC in SM



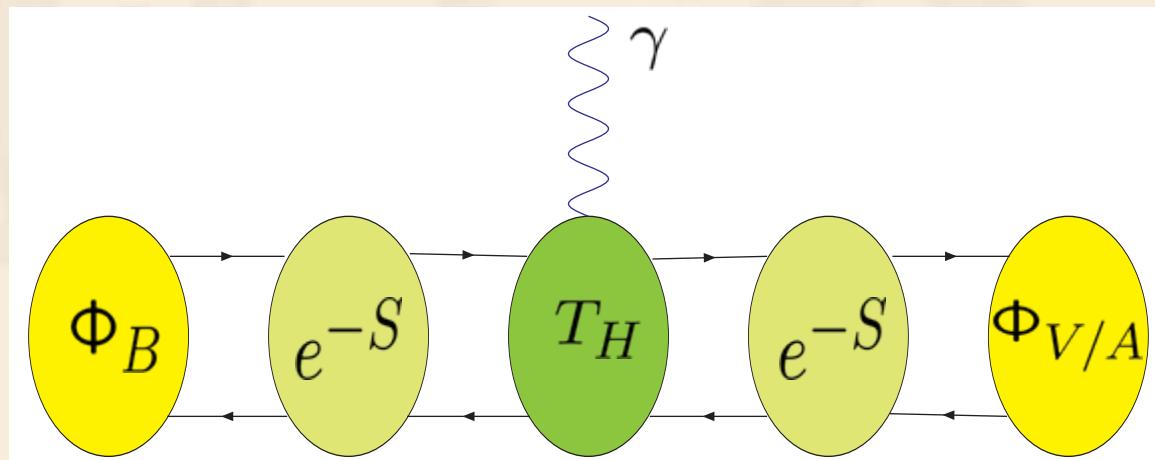
The dominate contribution is proportional to the transition form factor.



Main difficulty in theory for this type of decays



$B \rightarrow V/A \gamma$ in PQCD



$$\begin{aligned} \mathcal{M} = & \int_0^1 dx_1 dx_2 \int d^2 \vec{b}_1 d^2 \vec{b}_2 (2\pi)^2 \phi_B(x_1, \vec{b}_1, p_1, t) \\ & \times T_H(x_1, x_2, Q, \vec{b}_1, \vec{b}_2, t) \phi_V(x_2, \vec{b}_2, p_2, t) S_t(x_2) \exp[-S_B(t) - S_2(t)] \end{aligned}$$

For axial vector mesons:

$$\langle A(P_2, \epsilon^*) | \bar{q} \gamma^\mu \gamma_5 b | \bar{B}(P_1) \rangle = -\frac{2iA(q^2)}{m_B - m_A} \epsilon^{\mu\nu\rho\sigma} \epsilon_\nu^* P_{1\rho} P_{2\sigma},$$

$$\begin{aligned} \langle A(P_2, \epsilon^*) | \bar{q} \gamma^\mu b | \bar{B}(P_1) \rangle &= -2m_A V_0(q^2) \frac{\epsilon^* \cdot q}{q^2} q^\mu - (m_B - m_A) V_1(q^2) \left[\epsilon_\mu^* - \frac{\epsilon^* \cdot q}{q^2} q^\mu \right] \\ &\quad + V_2(q^2) \frac{\epsilon^* \cdot q}{m_B - m_A} \left[(P_1 + P_2)^\mu - \frac{m_B^2 - m_A^2}{q^2} q^\mu \right], \end{aligned}$$

$$\langle A(P_2, \epsilon^*) | \bar{q} \sigma^{\mu\nu} \gamma_5 q_\nu b | \bar{B}(P_1) \rangle = -2T_1(q^2) \epsilon^{\mu\nu\rho\sigma} \epsilon_\nu^* P_{1\rho} P_{2\sigma},$$

$$\begin{aligned} \langle A(P_2, \epsilon^*) | \bar{q} \sigma^{\mu\nu} q_\nu b | \bar{B}(P_1) \rangle &= -iT_2(q^2) \left[(m_B^2 - m_A^2) \epsilon^{*\mu} - (\epsilon^* \cdot q) (P_1 + P_2)^\mu \right] \\ &\quad - iT_3(q^2) (\epsilon^* \cdot q) \left[q^\mu - \frac{q^2}{m_B^2 - m_A^2} (P_1 + P_2)^\mu \right] \end{aligned}$$

At $q^2 = 0$, there is $2m_A V_0 = (m_B - m_A) V_1 - (m_B + m_A) V_2$.

Form Factors

For vector mesons:

$$\langle V(P_2, \epsilon^*) | \bar{q} \gamma^\mu b | \bar{B}(P_1) \rangle = -\frac{2V(q^2)}{m_B + m_V} \epsilon^{\mu\nu\rho\sigma} \epsilon_\nu^* P_{1\rho} P_{2\sigma},$$

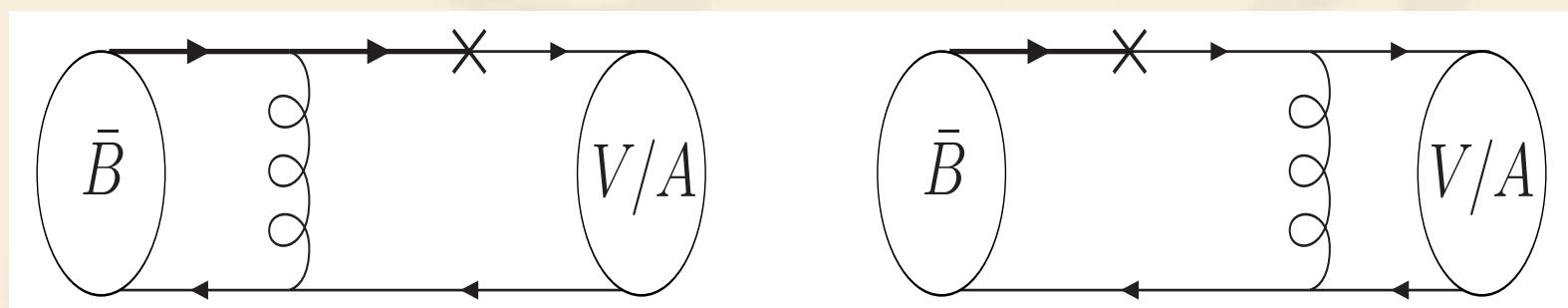
$$\begin{aligned} \langle V(P_2, \epsilon^*) | \bar{q} \gamma^\mu \gamma_5 b | \bar{B}(P_1) \rangle &= 2im_V A_0(q^2) \frac{\epsilon^* \cdot q}{q^2} q^\mu + i(m_B + m_V) A_1(q^2) \left[\epsilon_\mu^* - \frac{\epsilon^* \cdot q}{q^2} q^\mu \right] \\ &\quad - iA_2(q^2) \frac{\epsilon^* \cdot q}{m_B + m_V} \left[(P_1 + P_2)^\mu - \frac{m_B^2 - m_V^2}{q^2} q^\mu \right], \end{aligned}$$

$$\langle V(P_2, \epsilon^*) | \bar{q} \sigma^{\mu\nu} q_\nu b | \bar{B}(P_1) \rangle = -2iT_1(q^2) \epsilon^{\mu\nu\rho\sigma} \epsilon_\nu^* P_{1\rho} P_{2\sigma},$$

$$\begin{aligned} \langle V(P_2, \epsilon^*) | \bar{q} \sigma^{\mu\nu} \gamma_5 q_\nu b | \bar{B}(P_1) \rangle &= T_2(q^2) \left[(m_B^2 - m_V^2) \epsilon^{*\mu} - (\epsilon^* \cdot q)(P_1 + P_2)^\mu \right] \\ &\quad + T_3(q^2) (\epsilon^* \cdot q) \left[q^\mu - \frac{q^2}{m_B^2 - m_V^2} (P_1 + P_2)^\mu \right] \end{aligned}$$

At $q^2 = 0$, there is $2m_V A_0(0) = (m_B + m_V) A_1(0) - (m_B - m_V) A_2(0)$.

Contributions to form factor in PQCD



Mixing of the axial vector mesons

$$|K_1(1270)\rangle = |K_{1A}\rangle \sin \theta_K + |K_{1B}\rangle \cos \theta_K$$

$$|K_1(1400)\rangle = |K_{1A}\rangle \cos \theta_K - |K_{1B}\rangle \sin \theta_K$$

$$|f_1(1285)\rangle = |f_1\rangle \cos \theta_{3P_1} + |f_8\rangle \sin \theta_{3P_1}$$

$$|f_1(1420)\rangle = -|f_1\rangle \sin \theta_{3P_1} + |f_8\rangle \cos \theta_{3P_1}$$

$$|h_1(1170))\rangle = |h_1\rangle \cos \theta_{1P_1} + |h_8\rangle \sin \theta_{1P_1}$$

$$|h_1(1380)\rangle = -|h_1\rangle \sin \theta_{1P_1} + |h_8\rangle \cos \theta_{1P_1}$$

Kwei-Chou Yang, Nucl. Phys. B 776, 187 (2007)

form factors of $B \rightarrow V$

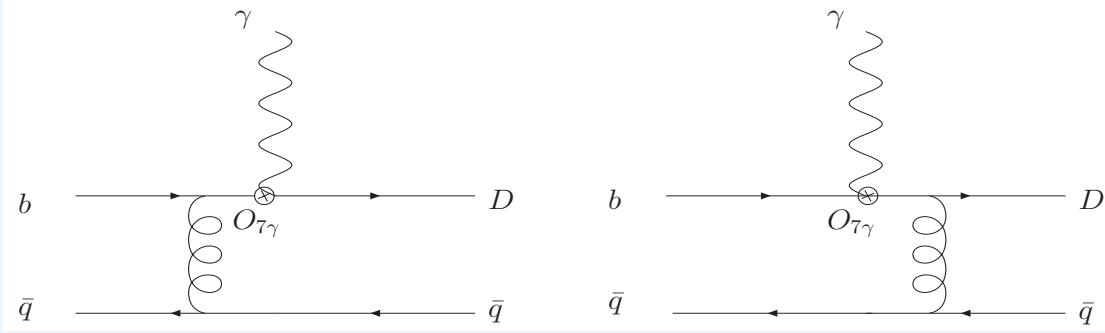
		$B \rightarrow \rho$	$B \rightarrow K^*$	$B \rightarrow \omega$	$B_s \rightarrow K^*$	$B_s \rightarrow \phi$
LFQM	V	0.27	0.31			
	A_0	0.28	0.31			
	A_1	0.22	0.26			
	A_2	0.20	0.24			
LCSR	V	0.323	0.411	0.293	0.311	0.434
	A_0	0.303	0.374	0.281	0.360	0.474
	A_1	0.242	0.292	0.219	0.233	0.311
	A_2	0.221	0.259	0.198	0.181	0.234
	T_2	0.267	0.333	0.242	0.260	0.349
LQCD	V	0.35				
	A_0	0.30				
	A_1	0.27				
	A_2	0.26				
	T_1		0.24			
SCET LCQM	V	0.298	0.339	0.275	0.323	0.329
	A_0	0.260	0.283	0.240	0.279	0.279
	A_1	0.227	0.248	0.209	0.228	0.232
	A_2	0.215	0.233	0.198	0.204	0.210
	$T_1 = T_2$	0.260	0.290	0.239	0.271	0.276
	T_3	0.184	0.194	0.168	0.165	0.170
This work	V	$0.21^{+0.05+0.00}_{-0.04-0.00}$	$0.25^{+0.05+0.00}_{-0.05-0.00}$	$0.20^{+0.04+0.00}_{-0.04-0.00}$	$0.21^{+0.04+0.00}_{-0.03-0.01}$	$0.25^{+0.05+0.00}_{-0.04-0.01}$
	A_0	$0.25^{+0.05+0.00}_{-0.05-0.01}$	$0.30^{+0.06+0.00}_{-0.05-0.01}$	$0.24^{+0.05+0.00}_{-0.04-0.01}$	$0.26^{+0.05+0.00}_{-0.04-0.01}$	$0.30^{+0.05+0.00}_{-0.05-0.01}$
	A_1	$0.17^{+0.04+0.00}_{-0.03-0.00}$	$0.19^{+0.04+0.00}_{-0.03-0.00}$	$0.15^{+0.03+0.00}_{-0.03-0.00}$	$0.16^{+0.03+0.00}_{-0.02-0.01}$	$0.18^{+0.03+0.00}_{-0.03-0.01}$
	A_2	$0.13^{+0.03+0.00}_{-0.02-0.00}$	$0.14^{+0.03+0.00}_{-0.03-0.00}$	$0.13^{+0.03+0.00}_{-0.02-0.00}$	$0.12^{+0.02+0.00}_{-0.02-0.01}$	$0.13^{+0.02+0.00}_{-0.02-0.01}$
	$T_1 = T_2$	$0.20^{+0.04+0.00}_{-0.04-0.00}$	$0.23^{+0.05+0.00}_{-0.04-0.00}$	$0.18^{+0.04+0.00}_{-0.03-0.00}$	$0.19^{+0.04+0.00}_{-0.03-0.01}$	$0.22^{+0.04+0.00}_{-0.04-0.01}$
	T_3	$0.13^{+0.03+0.00}_{-0.02-0.00}$	$0.13^{+0.03+0.00}_{-0.02-0.00}$	$0.12^{+0.03+0.00}_{-0.02-0.00}$	$0.11^{+0.02+0.00}_{-0.02-0.01}$	$0.12^{+0.02+0.00}_{-0.02-0.01}$

form factors of $B \rightarrow A$

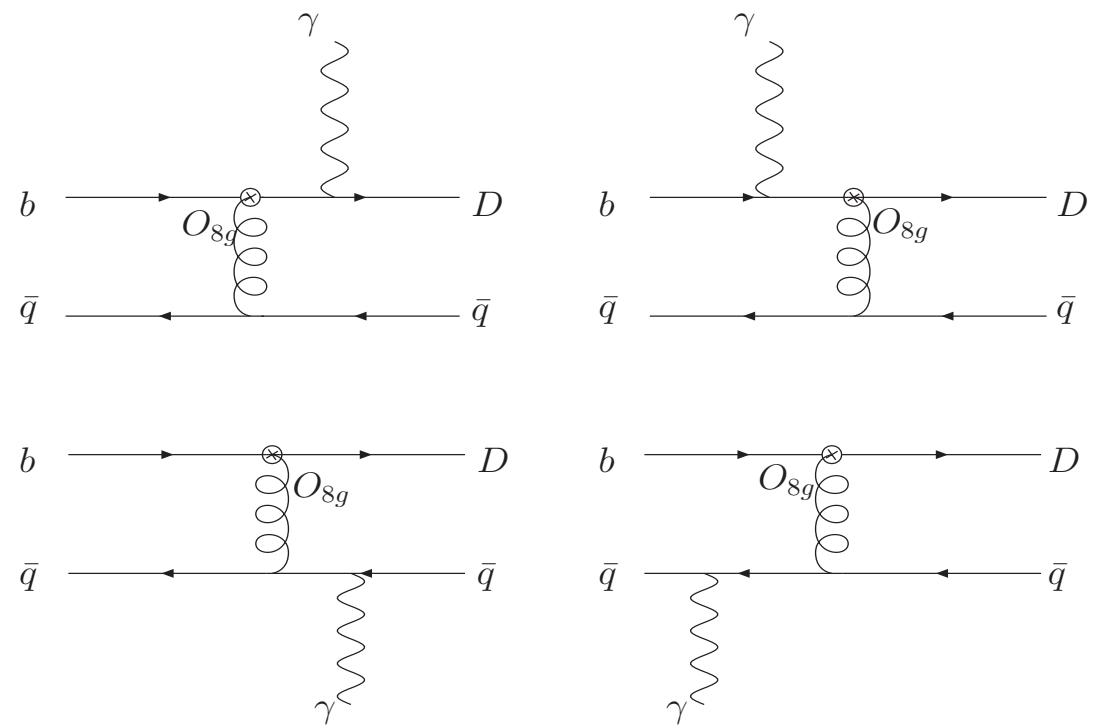
This work	$B \rightarrow a_1$	$B \rightarrow b_1$	$B \rightarrow K_{1A}$	$B \rightarrow K_{1B}$	$B_s \rightarrow K_{1A}$	$B_s \rightarrow K_{1B}$
A	$0.26^{+0.06+0.03}_{-0.05-0.03}$	$0.19^{+0.04+0.03}_{-0.03-0.02}$	$0.27^{+0.06+0.05}_{-0.05-0.05}$	$0.20^{+0.04+0.04}_{-0.04-0.04}$	$0.25^{+0.05+0.05}_{-0.04-0.05}$	$0.18^{+0.03+0.04}_{-0.03-0.04}$
V_0	$0.34^{+0.07+0.08}_{-0.06-0.08}$	$0.45^{+0.09+0.04}_{-0.08-0.04}$	$0.35^{+0.07+0.13}_{-0.06-0.13}$	$0.52^{+0.10+0.06}_{-0.09-0.07}$	$0.36^{+0.07+0.11}_{-0.06-0.12}$	$0.42^{+0.08+0.06}_{-0.07-0.06}$
V_1	$0.43^{+0.09+0.05}_{-0.08-0.05}$	$0.33^{+0.07+0.04}_{-0.06-0.04}$	$0.48^{+0.10+0.09}_{-0.09-0.09}$	$0.36^{+0.07+0.08}_{-0.06-0.08}$	$0.43^{+0.08+0.08}_{-0.07-0.08}$	$0.39^{+0.06+0.07}_{-0.05-0.07}$
V_2	$0.14^{+0.03+0.00}_{-0.03-0.00}$	$0.03^{+0.01+0.01}_{-0.00-0.01}$	$0.15^{+0.03+0.02}_{-0.03-0.02}$	$0.00^{+0.00+0.03}_{-0.00-0.03}$	$0.12^{+0.02+0.01}_{-0.02-0.01}$	$0.03^{+0.01+0.02}_{-0.01-0.02}$
$T_1(T_2)$	$0.34^{+0.07+0.05}_{-0.06-0.05}$	$0.27^{+0.06+0.03}_{-0.05-0.03}$	$0.37^{+0.08+0.08}_{-0.07-0.08}$	$0.29^{+0.06+0.06}_{-0.05-0.06}$	$0.34^{+0.06+0.07}_{-0.05-0.07}$	$0.26^{+0.05+0.05}_{-0.04-0.05}$
T_3	$0.19^{+0.04+0.01}_{-0.03-0.01}$	$0.06^{+0.01+0.02}_{-0.01-0.02}$	$0.20^{+0.04+0.02}_{-0.04-0.02}$	$0.03^{+0.01+0.00}_{-0.00-0.00}$	$0.17^{+0.03+0.02}_{-0.03-0.02}$	$0.06^{+0.01+0.03}_{-0.01-0.03}$
LFQM	$B \rightarrow a_1$	$B \rightarrow b_1$	$B \rightarrow K_{1A}$	$B \rightarrow K_{1B}$		
A	0.25	0.10	0.26	0.11		
V_0	0.13	0.39	0.14	0.41		
V_1	0.37	0.18	0.39	0.19		
V_2	0.18	-0.03	0.17	-0.05		
$T_1(T_2)$	--	--	0.11	0.13		
T_3	--	--	0.19	-0.07		

Amplitudes

$O_{7\gamma}$

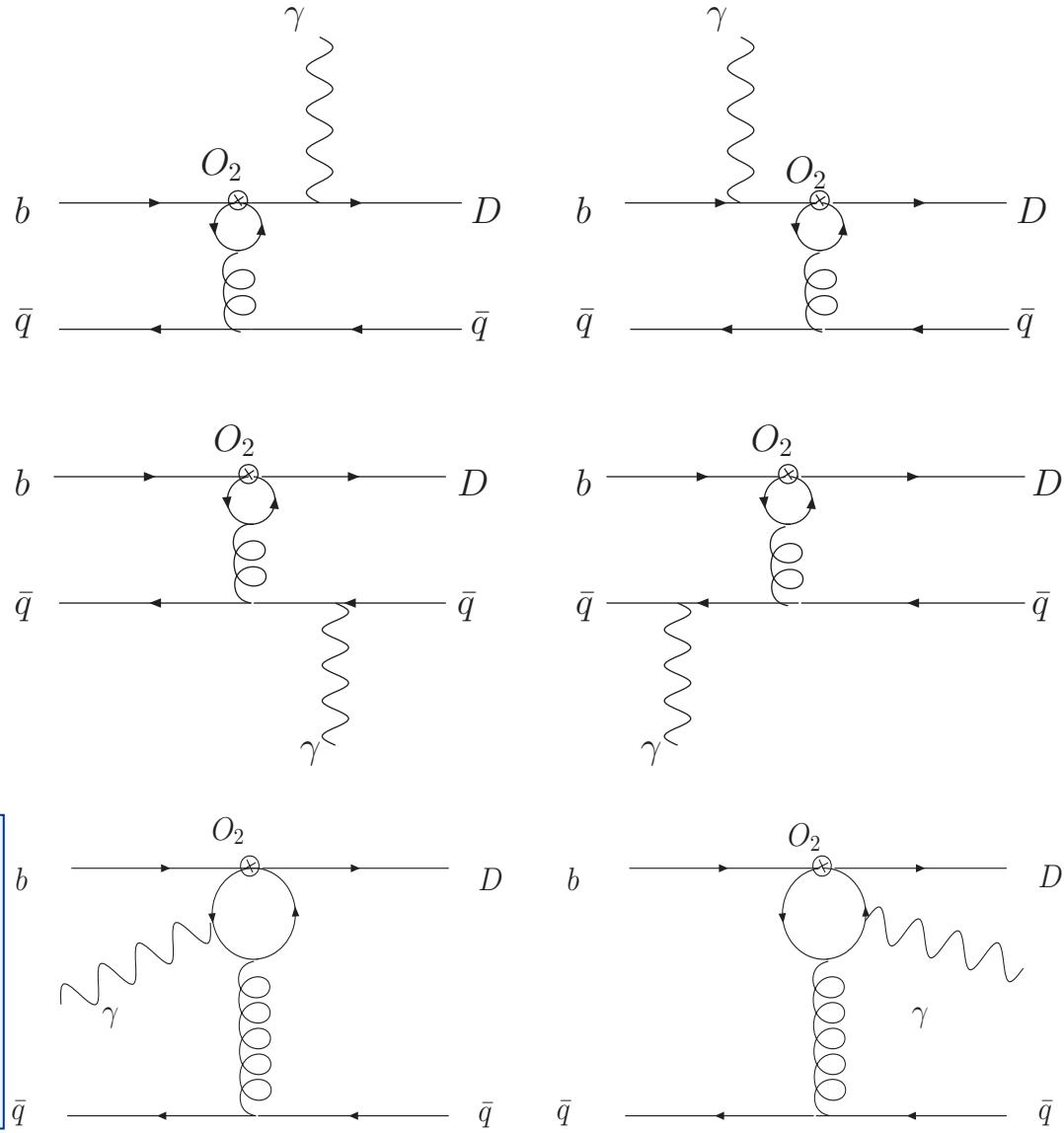


O_{8g}



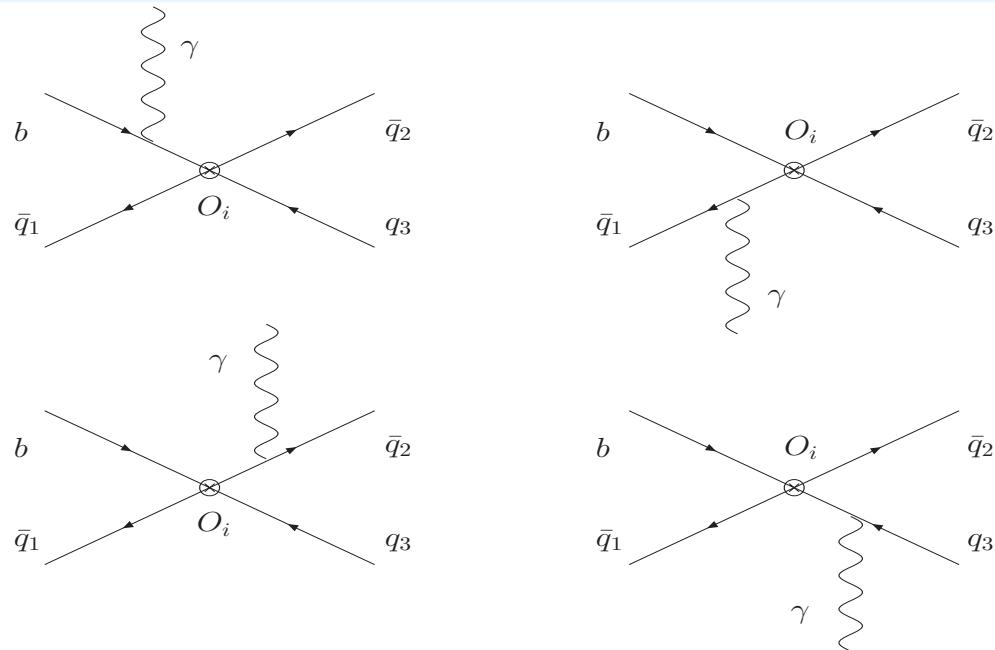
Loop contributions

Quark
line
photon
emission

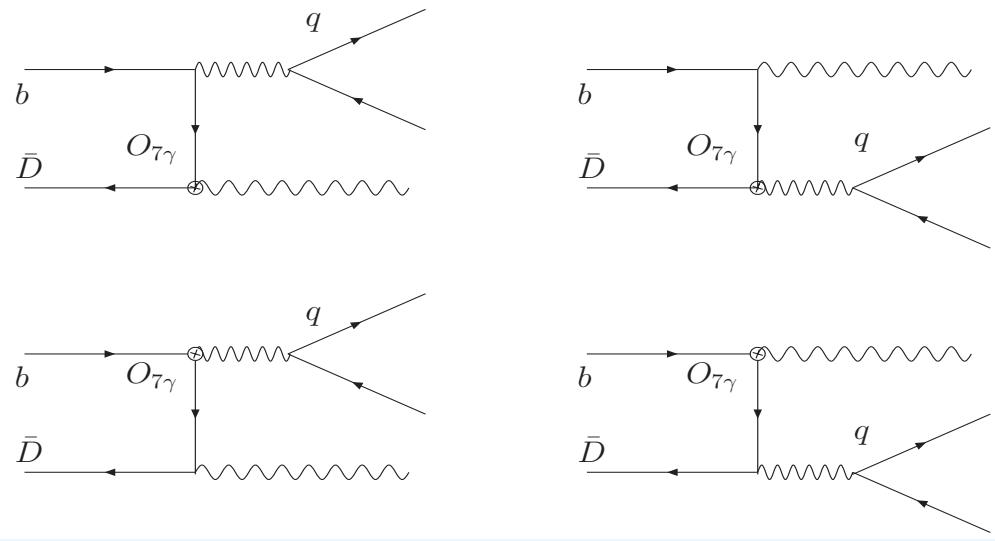


Loop line
photon
emission

Annihilation contributions



Two photon diagrams



Branch ratios

Branch ratios of $\bar{B} \rightarrow V\gamma$ Unit: 10^{-6}

Modes	QCDF	SCET	This work	Exp.
$B^- \rightarrow K^{*-} \gamma$	$53.3 \pm 13.5 \pm 5.8$	$46 \pm 12 \pm 4 \pm 2 \pm 1$	$35.8^{+17.6+5.4+1.1}_{-12.8-4.0-1.1}$	40.3 ± 2.6 [HFAG]
$\bar{B}^0 \rightarrow \bar{K}^{*0} \gamma$	$54.2 \pm 13.2 \pm 6.7$	$43 \pm 11 \pm 4 \pm 2 \pm 1$	$38.1^{+17.3+5.5+1.1}_{-12.7-3.8-1.1}$	40.1 ± 2.0 [HFAG]
$\bar{B}_s^0 \rightarrow \phi \gamma$	$39.4 \pm 10.7 \pm 5.3$	$43 \pm 11 \pm 3 \pm 3 \pm 1$	$35.8^{+13.7+4.9+1.1}_{-10.3-3.5-1.1}$	57^{+18+12}_{-15-11} [Belle]
Modes	QCDF	This work		Exp.
$B^- \rightarrow \rho^- \gamma$	$1.16 \pm 0.22 \pm 0.13$	$1.15^{+0.57+0.18+0.17}_{-0.39-0.11-0.09}$	$1.10^{+0.37}_{-0.33} \pm 0.09$ [BaBar]	$0.55^{+0.42+0.09}_{-0.36-0.08}$ [Belle]
$\bar{B}^0 \rightarrow \rho^0 \gamma$	$0.55 \pm 0.11 \pm 0.07$	$0.57^{+0.26+0.09+0.08}_{-0.19-0.06-0.04}$	$0.79^{+0.22}_{-0.20} \pm 0.06$ [BaBar]	$1.25^{+0.37+0.07}_{-0.33-0.06}$ [Belle]
$\bar{B}^0 \rightarrow \omega \gamma$	$0.44 \pm 0.09 \pm 0.05$	$0.51^{+0.23+0.08+0.08}_{-0.17-0.05-0.03}$	$0.40^{+0.24}_{-0.20} \pm 0.05$ [BaBar]	$0.56^{+0.34+0.05}_{-0.27-0.10}$ [Belle]
$\bar{B}_s^0 \rightarrow K^{*0} \gamma$	$1.26 \pm 0.25 \pm 0.18$	$1.11^{+0.42+0.15+0.16}_{-0.32-0.12-0.07}$		—
$\bar{B}^0 \rightarrow \phi \gamma$	—	$(7.5^{+2.8+2.1+1.1}_{-2.1-0.9-0.5}) \times 10^{-6}$		< 0.85 [HFAG]
$\bar{B}_s^0 \rightarrow \rho^0 \gamma$	—	$(1.7^{+0.4+0.1+0.0}_{-0.4-0.1-0.1}) \times 10^{-3}$		—
$\bar{B}_s^0 \rightarrow \omega \gamma$	—	$(1.8^{+0.4+0.1+0.1}_{-0.4-0.2-0.1}) \times 10^{-4}$		—

Branch ratios of $\bar{B} \rightarrow A\gamma$

Unit: 10^{-6}

$B^- \rightarrow a_1^-(1260)\gamma$	$3.0^{+1.6+0.4+0.4+0.8}_{-1.1-0.3-0.2-0.7}$
$\bar{B}^0 \rightarrow a_1^0(1260)\gamma$	$1.5^{+0.7+0.2+0.2+0.4}_{-0.5-0.2-0.1-0.4}$
$\bar{B}_s \rightarrow a_1^0(1260)\gamma$	$(2.1^{+0.6+0.3+0.1+0.0}_{-0.5-0.1-0.1-0.0}) \times 10^{-4}$
$B^- \rightarrow b_1^-(1235)\gamma$	$2.0^{+1.0+0.4+0.3+0.6}_{-0.7-0.3-0.1-0.5}$
$\bar{B}^0 \rightarrow b_1^0(1235)\gamma$	$1.1^{+0.5+0.2+0.2+0.3}_{-0.3-0.1-0.1-0.2}$
$\bar{B}_s \rightarrow b_1^0(1235)\gamma$	$(5.4^{+1.0+6.4+0.3+2.1}_{-0.9-2.5-0.2-1.8}) \times 10^{-5}$

Unit: 10^{-6}

Modes	$\theta_K = 45^\circ$	$\theta_K = -45^\circ$
$B^- \rightarrow K_1^-(1270)\gamma$	$134^{+68+21+4+41}_{-49-18-4-38}$	$1.4^{+1.2+0.3+0.0+5.0}_{-0.7-0.6-0.0-2.0}$
$\bar{B}^0 \rightarrow \bar{K}_1^0(1270)\gamma$	$141^{+64+19+4+45}_{-48-18-4-41}$	$1.4^{+0.9+0.3+0.0+5.4}_{-0.6-0.5-0.0-1.9}$
$B^- \rightarrow K_1^-(1400)\gamma$	$1.4^{+1.2+0.3+0.0+5.0}_{-0.7-0.6-0.0-2.0}$	$134^{+68+21+4+41}_{-49-18-4-38}$
$\bar{B}^0 \rightarrow \bar{K}_1^0(1400)\gamma$	$1.4^{+0.9+0.3+0.0+5.4}_{-0.6-0.5-0.0-1.9}$	$141^{+64+19+4+45}_{-48-18-4-41}$
$\bar{B}_s \rightarrow K_1^0(1270)\gamma$	$0.19^{+0.07+0.02+0.02+0.34}_{-0.06-0.03-0.01-0.22}$	$0.38^{+0.24+0.09+0.07+0.44}_{-0.15-0.07-0.03-0.32}$
$\bar{B}_s \rightarrow K_1^0(1400)\gamma$	$0.38^{+0.24+0.09+0.07+0.44}_{-0.15-0.07-0.03-0.32}$	$0.19^{+0.07+0.02+0.02+0.34}_{-0.06-0.03-0.01-0.22}$
Modes	$\theta_{3P_1} = 38^\circ$	$\theta_{3P_1} = 50^\circ$
$\bar{B}^0 \rightarrow f_1(1285)\gamma$	$1.7^{+0.8+0.2+0.2+0.5}_{-0.6-0.2-0.1-0.4}$	$1.6^{+0.7+0.2+0.2+0.4}_{-0.5-0.2-0.1-0.4}$
$\bar{B}^0 \rightarrow f_1(1420)\gamma$	$(4.9^{+2.3+0.6+0.7+3.9}_{-1.7-1.1-0.3-2.7}) \times 10^{-3}$	$0.11^{+0.05+0.01+0.02+0.04}_{-0.04-0.02-0.01-0.04}$
$\bar{B}_s^0 \rightarrow f_1(1285)\gamma$	$0.11^{+0.05+0.01+0.00+0.03}_{-0.04-0.01-0.00-0.03}$	$3.8^{+1.6+0.4+0.1+0.7}_{-1.2-0.4-0.1-0.7}$
$\bar{B}_s^0 \rightarrow f_1(1420)\gamma$	$61.9^{+24.5+5.5+1.8+17.4}_{-18.9-6.0-1.8-15.5}$	$58.2^{+22.9+5.1+1.6+16.7}_{-17.7-5.6-1.7-14.8}$
Modes	$\theta_{1P_1} = 10^\circ$	$\theta_{1P_1} = 45^\circ$
$\bar{B}^0 \rightarrow h_1(1170)\gamma$	$0.99^{+0.43+0.16+0.14+0.24}_{-0.33-0.13-0.06-0.21}$	$1.24^{+0.55+0.20+0.18+0.31}_{-0.41-0.16-0.08-0.27}$
$\bar{B}^0 \rightarrow h_1(1380)\gamma$	$0.28^{+0.12+0.05+0.04+0.07}_{-0.09-0.04-0.02-0.06}$	$(2.0^{+0.8+0.3+0.3+0.3}_{-0.7-0.3-0.1-0.3}) \times 10^{-2}$
$\bar{B}_s^0 \rightarrow h_1(1170)\gamma$	$7.9^{+2.9+1.0+0.2+1.8}_{-2.2-0.7-0.2-1.6}$	$2.3^{+0.9+0.3+0.1+0.7}_{-0.7-0.3-0.1-0.6}$
$\bar{B}_s^0 \rightarrow h_1(1380)\gamma$	$44.4^{+16.8+5.6+1.3+11.0}_{-12.8-4.1-1.3-9.7}$	$50.0^{+18.8+6.3+1.5+12.2}_{-14.3-4.5-1.5-10.7}$

CP Violation

Direct CPV

$$A_{\text{CP}}^{\text{dir}} \equiv \frac{\mathcal{BR}(\bar{B} \rightarrow \bar{V}\gamma) - \mathcal{BR}(B \rightarrow V\gamma)}{\mathcal{BR}(\bar{B} \rightarrow \bar{V}\gamma) + \mathcal{BR}(B \rightarrow V\gamma)}$$

Mixing -induced CPV

$$\begin{aligned} \Gamma(B^0(t) \rightarrow f) = & e^{-\Gamma t} \bar{\Gamma}(B \rightarrow f) \left[\cosh\left(\frac{\Delta\Gamma t}{2}\right) + \color{red}H_f\sinh\left(\frac{\Delta\Gamma t}{2}\right) \right. \\ & \left. - A_{\text{CP}}^{\text{dir}} \cos(\Delta m t) - \color{red}S_f \sin(\Delta m t) \right] \end{aligned}$$

$\bar{B} \rightarrow V\gamma$ Unit: %

$B^- \rightarrow \rho^-\gamma$	$12.8^{+0.8+2.9+0.8}_{-0.3-1.8-0.8}$
$\bar{B}^0 \rightarrow \rho^0\gamma$	$12.4^{+0.2+1.8+0.5}_{-0.4-2.4-0.9}$
$\bar{B}^0 \rightarrow \omega\gamma$	$12.1^{+0.0+1.8+0.5}_{-0.2-2.4-0.8}$
$\bar{B}_s^0 \rightarrow K^{*0}\gamma$	$12.7^{+0.1+1.6+0.5}_{-0.5-2.3-0.9}$



$b \rightarrow d\gamma$

$$B^- \rightarrow K^{*-}\gamma \quad -0.4 \pm 0.0 \pm 0.1 \pm 0.0$$

$$\bar{B}^0 \rightarrow \bar{K}^{*0}\gamma \quad -0.3^{+0.0+0.0+0.0}_{-0.0-0.0-0.0}$$

$$\bar{B}_s^0 \rightarrow \rho^0\gamma \quad -0.1^{+0.0+0.3+0.0}_{-0.0-0.1-0.0}$$

$$\bar{B}_s^0 \rightarrow \omega\gamma \quad -0.3^{+0.0+0.9+0.0}_{-0.0-0.5-0.0}$$

$$\bar{B}_s^0 \rightarrow \phi\gamma \quad -0.3^{+0.0+0.0+0.0}_{-0.0-0.0-0.0}$$



$b \rightarrow s\gamma$

$\bar{B} \rightarrow A\gamma$ Unit: %

$B^- \rightarrow a_1^-(1260)\gamma$	$11.2^{+2.3+3.0+0.9+2.7}_{-0.5-2.4-0.8-1.3}$
$\bar{B}^0 \rightarrow a_1^0(1260)\gamma$	$3.8^{+0.3+0.3+0.2+0.4}_{-0.5-0.5-0.3-0.7}$
$B^- \rightarrow b_1^-(1235)\gamma$	$16.0^{+1.3+4.2+0.7+1.7}_{-0.5-2.7-1.1-0.7}$
$\bar{B}^0 \rightarrow b_1^0(1235)\gamma$	$11.0^{+0.2+1.9+0.5+0.3}_{-0.3-2.5-0.7-0.2}$
$\bar{B}_s \rightarrow a_1^0(1260)\gamma$	$0.8^{+0.1+0.8+0.1+0.0}_{-0.1-1.5-0.0-0.0}$
$\bar{B}_s \rightarrow b_1^0(1235)\gamma$	$-0.5^{+0.0+2.7+0.0+0.0}_{-0.0-1.5-0.0-0.0}$



$b \rightarrow d\gamma$



$b \rightarrow s\gamma$

Modes	$\theta_K = 45^\circ$	$\theta_K = -45^\circ$
$B^- \rightarrow K_1^-(1270)\gamma$	$-0.6^{+0.0+0.2+0.0+0.1}_{-0.0-0.1-0.0-0.1}$	$-3.8^{+0.7+1.1+1.8+4.0}_{-1.3-0.3-0.3-13.0}$
$\bar{B}^0 \rightarrow \bar{K}_1^0(1270)\gamma$	$-0.2 \pm 0.0 \pm 0.0 \pm 0.0 \pm 0.0$	$0.1^{+0.0+0.1+0.0+2.2}_{-0.1-0.3-0.0-0.4}$
$B^- \rightarrow K_1^-(1400)\gamma$	$-3.8^{+0.7+1.1+1.8+4.0}_{-1.3-0.3-0.3-13.0}$	$-0.6^{+0.0+0.2+0.0+0.1}_{-0.0-0.1-0.0-0.1}$
$\bar{B}^0 \rightarrow \bar{K}_1^0(1400)\gamma$	$0.1^{+0.0+0.1+0.0+2.2}_{-0.1-0.3-0.0-0.4}$	$-0.2 \pm 0.0 \pm 0.0 \pm 0.0 \pm 0.0$
$B_s \rightarrow K_1^0(1270)\gamma$	$-8.4^{+0.0+0.5+0.4+5.1}_{-2.9-3.4-0.4-11.2}$	$-3.1^{+3.9+4.0+0.8+8.6}_{-0.1-3.1-0.6-14.1}$
$\bar{B}_s \rightarrow \bar{K}_1^0(1400)\gamma$	$-3.1^{+3.9+4.0+0.8+8.6}_{-0.1-3.1-0.6-14.1}$	$-8.4^{+0.0+0.5+0.4+5.1}_{-2.9-3.4-0.4-11.2}$
Modes	$\theta_{3P_1} = 38^\circ$	$\theta_{3P_1} = 50^\circ$
$B^0 \rightarrow f_1(1285)\gamma$	$3.4^{+0.6+0.8+0.2+0.7}_{-0.1-0.5-0.2-0.1}$	$3.4^{+0.7+0.8+0.2+0.8}_{-0.1-0.4-0.2-0.1}$
$\bar{B}^0 \rightarrow f_1(1420)\gamma$	$7.1^{+0.0+0.7+0.3+0.0}_{-3.1-7.7-0.5-2.3}$	$4.1^{+0.1+0.5+0.2+0.1}_{-0.3-1.9-0.3-0.4}$
$\bar{B}_s^0 \rightarrow f_1(1285)\gamma$	$-0.1^{+0.3+0.1+0.0+0.1}_{-0.0-0.1-0.0-0.2}$	$-0.2^{+0.1+0.0+0.0+0.0}_{-0.0-0.1-0.0-0.0}$
$B_s^0 \rightarrow f_1(1420)\gamma$	$-0.2 \pm 0.0 \pm 0.0 \pm 0.0 \pm 0.0$	$-0.2 \pm 0.0 \pm 0.0 \pm 0.0 \pm 0.0$
Modes	$\theta_{1P_1} = 10^\circ$	$\theta_{1P_1} = 45^\circ$
$\bar{B}^0 \rightarrow h_1(1170)\gamma$	$10.2^{+0.0+1.4+0.4+0.0}_{-0.9-2.5-0.7-0.4}$	$10.1^{+0.1+1.7+0.4+0.2}_{-0.5-2.3-0.7-0.3}$
$\bar{B}^0 \rightarrow h_1(1380)\gamma$	$9.8^{+0.8+2.4+0.4+1.1}_{-0.0-2.0-0.7-0.0}$	$11.3^{+0.0+0.0+0.5+0.0}_{-5.1-4.2-0.7-3.5}$
$\bar{B}_s^0 \rightarrow h_1(1170)\gamma$	$-0.2 \pm 0.0 \pm 0.0 \pm 0.0 \pm 0.0$	$-0.1^{+0.0+0.0+0.0+0.0}_{-0.0-0.1-0.0-0.0}$
$B_s^0 \rightarrow h_1(1380)\gamma$	$-0.2 \pm 0.0 \pm 0.0 \pm 0.0 \pm 0.0$	$-0.2 \pm 0.0 \pm 0.0 \pm 0.0 \pm 0.0$

Iso-spin and U-spin asymmetry

$$A(\rho, \omega) = \frac{\bar{\Gamma}(B^0 \rightarrow \omega\gamma)}{\bar{\Gamma}(B^0 \rightarrow \rho^0\gamma)} - 1$$

$$-0.11^{+0.01+0.01+0.00}_{-0.00-0.00-0.00}$$

$$A(\rho, \omega) = \frac{\bar{\Gamma}(B^0 \rightarrow \omega\gamma)}{\bar{\Gamma}(B^0 \rightarrow \rho^0\gamma)} - 1$$

$$0.06^{+0.03+0.01+0.04}_{-0.03-0.01-0.02}$$

$$A_I(K^*) = \frac{\bar{\Gamma}(\bar{B}^0 \rightarrow \bar{K}^{*0}\gamma) - \bar{\Gamma}(B^\pm \rightarrow K^{*\pm}\gamma)}{\bar{\Gamma}(\bar{B}^0 \rightarrow \bar{K}^{*0}\gamma) + \bar{\Gamma}(B^\pm \rightarrow K^{*\pm}\gamma)}$$

$$0.06^{+0.02+0.01+0.00}_{-0.01-0.00-0.00}$$

$$\Delta \equiv A_{CP}(B^- \rightarrow K^{*-}\gamma) - A_{CP}(B^- \rightarrow \rho^-\gamma) \times \frac{\mathcal{BR}(B^- \rightarrow \rho^-\gamma)}{\mathcal{BR}(B^- \rightarrow K^{*-}\gamma)}$$

$$(-8.4^{+0.4+1.3+0.3}_{-0.8-2.3-0.6}) \times 10^{-3}$$

Summary

- ❖ We calculated the radiative decays of B mesons in PQCD approach.
- ❖ Most our results are consistent with the experiments within the uncertainties.
- ❖ The results of the axial vector mesons are sensitive to the mixing angles.
- ❖ Some of our results are confronted with the forthcoming experiments.
- ❖ The iso-spin symmetry and U-spin symmetry breaking effects are small.

Thank you!